Towards Verification of Linux Kernel Code

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 - Existing tools handle these issues more or less well (Smatch, Coccinelle, Coverity, etc.)
- Some depend on an algorithm, and are completely context specific:
 - Maybe the Linux kernel is a candidate for verification?

A challenge

Verification is really hard...

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- Sometimes to optimize existing code.
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- Sometimes to optimize existing code.
- Sometimes to fix bugs.
- Sometimes introducing bugs. :(

An idea

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- Maybe we could define pre and post conditions for one version and reuse them on new versions?

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- Achieve uptake from the Linux kernel community?

What we do:

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- Write dummy definitions in C for external functions, as needed.
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What we don't do:

- No consideration of concurrency.
- No consideration of hidden memory issues (aliasing, null pointers, use after free, etc.).
- These are hard issues, but developers can make mistakes without them.

A case study: should_we_balance

Goal:

Should a core should try to steal tasks during load balancing?

Starting point:

- Patch first proposed in August 2013.
- Extracted from scattered existing code.
- First patch was buggy.
- First released in Linux v3.12.

Subsequent history:

- 10 variants over time (+1 proposed by Keisuke).
- Several recent optimizations.

The original definition

```
static int should we balance(struct lb_env *env) {
        struct sched group *sg = env->sd->groups:
        struct cpumask *sg_cpus, *sg_mask;
        int cpu, balance cpu = -1:
        if (env->idle == CPU_NEWLY_IDLE)
                return 1:
        sg cpus = sched group cpus(sg);
        sg_mask = sched_group_mask(sg);
        for each cpu and (cpu, sg cpus, env->cpus) {
                if (!cpumask_test_cpu(cpu, sg_mask) || !idle_cpu(cpu))
                        continue:
                balance_cpu = cpu;
                break:
        if (balance cpu == -1)
                balance_cpu = group_balance_cpu(sg);
        return balance_cpu != env->dst_cpu; // != should be ==
```

Input: env describes the core that wants to steal tasks

```
static int should we balance(struct lb env *env) {
        struct sched group *sg = env->sd->groups:
        struct cpumask *sg_cpus, *sg_mask;
        int cpu, balance cpu = -1:
        if (env->idle == CPU_NEWLY_IDLE)
                return 1:
        sg cpus = sched group cpus(sg);
        sg mask = sched group mask(sg);
        for each cpu and (cpu, sg cpus, env->cpus) {
                if (!cpumask_test_cpu(cpu, sg_mask) || !idle_cpu(cpu))
                        continue:
                balance cpu = cpu:
                break:
        if (balance cpu == -1)
                balance cpu = group balance cpu(sg):
        return balance_cpu != env->dst_cpu; // != should be ==
```

If the core is newly idle, it can always steal

```
static int should we balance(struct lb_env *env) {
        struct sched group *sg = env->sd->groups:
        struct cpumask *sg_cpus, *sg_mask;
        int cpu, balance cpu = -1:
        if (env->idle == CPU_NEWLY_IDLE)
                return 1:
        sg cpus = sched group cpus(sg);
        sg_mask = sched_group_mask(sg);
        for each cpu and (cpu, sg cpus, env->cpus) {
                if (!cpumask_test_cpu(cpu, sg_mask) || !idle_cpu(cpu))
                        continue:
                balance cpu = cpu:
                break:
        if (balance cpu == -1)
                balance cpu = group balance cpu(sg):
        return balance_cpu != env->dst_cpu; // != should be ==
```

Otherwise, find the core that is allowed to steal

```
static int should we balance(struct lb_env *env) {
        struct sched group *sg = env->sd->groups:
        struct cpumask *sg_cpus, *sg_mask;
        int cpu, balance_cpu = -1;
        if (env->idle == CPU_NEWLY_IDLE)
                 return 1:
        sg cpus = sched group cpus(sg);
        sg mask = sched group mask(sg);
        for each cpu and(cpu, sg cpus, env->cpus) {
                 if (!cpumask_test_cpu(cpu, sg_mask) | | !idle_cpu(cpu))
                         continue:
                 balance cpu = cpu:
                break:
        if (balance cpu == -1)
                balance cpu = group balance cpu(sg):
        return balance_cpu != env->dst_cpu; // != should be ==
```

The first idle core is allowed to steal

```
static int should we balance(struct lb_env *env) {
        struct sched group *sg = env->sd->groups:
        struct cpumask *sg_cpus, *sg_mask;
        int cpu, balance cpu = -1:
        if (env->idle == CPU_NEWLY_IDLE)
                return 1:
        sg cpus = sched group cpus(sg);
        sg_mask = sched_group_mask(sg);
        for each cpu and (cpu, sg cpus, env->cpus) {
                if (!cpumask_test_cpu(cpu, sg_mask) || !idle_cpu(cpu))
                        continue:
                balance cpu = cpu:
                break:
        if (balance cpu == -1)
                balance cpu = group balance cpu(sg):
        return balance_cpu != env->dst_cpu; // != should be ==
```

If no core is idle, a designated core is allowed to steal

```
static int should we balance(struct lb_env *env) {
        struct sched group *sg = env->sd->groups:
        struct cpumask *sg_cpus, *sg_mask;
        int cpu, balance cpu = -1:
        if (env->idle == CPU_NEWLY_IDLE)
                return 1:
        sg cpus = sched group cpus(sg);
        sg mask = sched group mask(sg);
        for each cpu and (cpu, sg cpus, env->cpus) {
                if (!cpumask_test_cpu(cpu, sg_mask) || !idle_cpu(cpu))
                        continue:
                balance cpu = cpu:
                break:
        if (balance cpu == -1)
                balance cpu = group balance cpu(sg):
        return balance_cpu != env->dst_cpu; // != should be ==
```

Is the core that is allowed to steal the current one?

```
static int should we balance(struct lb_env *env) {
        struct sched group *sg = env->sd->groups:
        struct cpumask *sg_cpus, *sg_mask;
        int cpu, balance cpu = -1:
        if (env->idle == CPU_NEWLY_IDLE)
                return 1:
        sg cpus = sched group cpus(sg);
        sg_mask = sched_group_mask(sg);
        for each cpu and (cpu, sg cpus, env->cpus) {
                if (!cpumask_test_cpu(cpu, sg_mask) || !idle_cpu(cpu))
                        continue:
                balance cpu = cpu:
                break:
        if (balance cpu == -1)
                balance cpu = group balance cpu(sg):
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```

Key properties

For a given environment env,

- Uniqueness If two non-newly idle cores call should_we_balance, then at most one of them should get a positive result.
- Existence should_we_balance should return true for some core on the machine.

Key properties

For a given environment env,

- Uniqueness If two non-newly idle cores call should_we_balance,
 then at most one of them should get a positive result.
- Existence should_we_balance should return true for some core on the machine.

What to prove?

- Frama-C proves postconditions from preconditions.
 - Describes function semantics in terms of the input-output behavior.
- Our key properties are somewhat different, but start with that.

Initial version (verification expert): pre and post conditions

```
1*0
... // data validity, no side effects
behavior newly idle:
  assumes env->idle == CPU NEWLY IDLE;
  ensures \result:
behavior not newly idle1:
  assumes env->idle != CPU NEWLY IDLE;
  assumes \exists integer i; relevant(i, env) && idle cpu(i);
  ensures \forall integer i:
    relevant(i, env) ==> idle cpu(i) ==>
    (\forall integer j: 0 \le j \le i ==> relevant(j, env) ==> !idle cpu(j)) ==>
    (\result <==> env->dst cpu != i);
behavior not newly idle2:
  assumes env->idle != CPU NEWLY IDLE:
 assumes \forall integer i: relevant(i, env) ==> !idle cru(i):
  ensures \result <==> group balance cpu(env->sd->groups) != env->dst cpu:
complete behaviors:
disjoint behaviors;
*/
```

Initial version (verification expert): loop invariants

```
static int should we balance(struct 1b env *env)
        sg_cpus = sched_group_cpus(sg);
        sg_mask = sched_group_mask(sg);
        1*0
          loop invariant 0 <= cpu <= small cpumask bits:
          loop invariant \forall integer j: 0 <= j < cpu ==> relevant(j, env) ==> !idle cpu(j);
          loop assigns cpu:
          loop variant small cpumask bits - cpu;
        for each cpu and (cpu, sg cpus, env->cpus) {
                if (!cpumask_test_cpu(cpu, sg_mask) || !idle_cpu(cpu))
                        continue:
                balance_cpu = cpu:
                break:
```

Change types and proof impact

#	Commmit id	Date	Release	Impact
0	23f0d2093c78	Aug. 2013	_	create the function
1	b0cff9d88ce2	Sep. 2013	v3.12	replace != by ==
2	af218122b103	May 2017	_	eliminate a redundant function call
3	e5c14b1fb892	May 2017	v4.13	rename a functiom
4	024c9d2faebd	Oct. 2017	v4.14	check validity of the stealing CPU
5	97fb7a0a8944	Mar. 2018	v4.17	improve comments
6	64297f2b03cc	Apr. 2020	v5.8	return early on finding an idle core
7	792b9f65a568	Jun. 2022	v6.0	abort if tasks are detected on a newly idle CPU
8	b1bfeab9b002	Jul. 2023	_	prefer fully idle cores
9	f8858d96061f	Sep. 2023	v6.6	remove non-idle hyperthreads from the CPU mask
10	6d7e4782bcf5	Oct. 2023	v6.8	change a condition of the selection algorithm

Red versions contain bugs.

Question:

As the code changes, can developers update the specifications accordingly?

Change types and proof impact: No impact

Changes in comments clearly have no impact on the proof.

Change types and proof impact: No impact

Changes in comments clearly have no impact on the proof.

Code changes may also have no impact on the proof.

```
static int should_we_balance(struct lb_env *env)
       struct sched_group *sg = env->sd->groups;
       int cpu, balance cpu = -1;
       int cpu;
       for_each_cpu_and(cpu, group_balance_mask(sg), env->cpus) {
               if (!idle_cpu(cpu))
                       continue:
               balance_cpu = cpu;
               break:
               return cpu == env->dst_cpu;
       if (balance cpu == -1)
               balance cpu = group balance cpu(sg):
       return balance_cpu == env->dst_cpu;
       return group balance cpu(sg) == env->dst cpu:
```

Change types and proof impact: new conditions

```
static int should_we_balance(struct lb_env *env)
       struct sched_group *sg = env->sd->groups;
       int cpu, balance cpu = -1:
       if (!cpumask_test_cpu(env->dst_cpu, env->cpus))
               return 0;
       if (env->idle == CPU_NEWLY_IDLE)
               return 1;
       for_each_cpu_and(cpu, group_balance_mask(sg), env->cpus) {
               if (!idle_cpu(cpu))
                       continue:
               balance_cpu = cpu;
               break:
       if (balance cpu == -1)
               balance cpu = group balance cpu(sg):
       return balance_cpu == env->dst_cpu;
```

Change types and proof impact: new conditions

```
+behavior race condition:
+ assumes !env->cpus->bits[env->dst cpu]:
+ ensures !\result:
behavior newly_idle:
  assumes env->idle == CPU NEWLY IDLE:
+ assumes env->cpus->bits[env->dst_cpu];
  ensures \result;
 behavior not_newly_idle1:
  assumes env->idle != CPU_NEWLY_IDLE;
+ assumes env->cpus->bits[env->dst_cpu];
   assumes \exists integer i: relevant(i, env) && idle cpu(i):
   ensures \forall integer i:
    relevant(i, env) ==> idle cpu(i) ==>
     (\forall integer j: 0 <= j < i ==> relevant(j, env) ==> !idle_cpu(j)) ==>
     (\result <==> env->dst_cpu == i):
 behavior not newly idle2:
  assumes env->idle != CPU_NEWLY_IDLE;
+ assumes env->cpus->bits[env->dst cpu]:
   assumes \forall integer i; relevant(i, env) ==> !idle_cpu(i);
   ensures \result <==> group_balance_cpu(env->sd->groups) == env->dst_cpu;
```

Change types and proof impact: Bridge to the old specifications using axioms?

Code change:

```
commit af218122b103900fa33d408aea0c2468791e698c
Author: Peter Zijlstra <peterz@infradead.org>
Date: Mon May 1 08:51:05 2017 +0200

sched/topology: Simplify sched_group_mask() usage

While writing the comments, it occurred to me that:

sg_cpus & sg_mask == sg_mask

at least conceptually; the !overlap case sets the all 1s mask. If we correct that we can simplify things and directly use sg_mask.
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Specification change:

sched_group_mask(groups)->bits[i] ==> sched_group_cpus(groups)->bits[i]
as an axiom?

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    sg_cpus & sg_mask == sg_mask
    at least conceptually; the !overlap case sets the all 1s mask. If we correct that we can simplify things and directly use sg_mask.
```

Specification change:

- sched_group_mask(groups)->bits[i] ==> sched_group_cpus(groups)->bits[i]
 as an axiom?
- Too much proof clutter.

Drop sched_group_cpus(groups)->bits[i] as done in the code.

- Sensitive to hyperthreads.
- Avoid a core whose hyperthread is occupied, but keep it as a fallback.

Specification change:

```
/*@
loop invariant 0 <= cpu <= small_cpumask_bits;

loop invariant \forall integer j; 0 <= j < cpu ==> relevant(j, env) ==> !idle_cpu(j);

loop assigns cpu;

loop invariant env->sd->flags & SD_SHARE_CPUCAPACITY ==> idle_smt == -1;

loop invariant idle_smt == -1 ==> \forall integer j; 0 <= j < cpu ==> relevant(j, env) ==> !idle_cpu(j);

loop invariant idle_smt != -1 ==> 0 <= idle_smt < cpu && relevant(idle_smt, env) && idle_cpu(idle_smt);

loop invariant idle_smt != -1 ==> \forall integer j; 0 <= j < idle_smt ==> relevant(j, env) ==> !idle_cpu(j);

loop invariant idle_smt != -1 ==> \forall integer j; idle_smt <= j < cpu ==> relevant(j, env) ==> !idle_core(j);

loop assigns cpu, idle_smt;

loop variant small_cpumask_bits - cpu;

*/
```

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Months of work... One assert needed.

Bugs found and optimization opportunities

An older behavior:

```
behavior not_newly_idle1:
    assumes env->idle != CPU_NEWLY_IDLE;
    assumes env->cpus->bits[env->dst_cpu];
    assumes \exists integer i; relevant(i, env) && idle_cpu(i);
    ensures \forall integer i; relevant(i, env) ==> idle_cpu(i) ==>
        (\forall integer j; 0 <= j < i ==> relevant(j, env) ==> !idle_cpu(j)) ==>
        (\result <==> env->dst_cpu == i);
```

A newer behavior: (bug introduced)

Bugs found and optimization opportunities

Optimization opportunity: (ifdefs elided)

No changes needed to the specifications!

Assessment

Work estimate:

- Maybe 1.5 months for versions 0 8. ✓
- 3.5 months for version 9 (cpumask_andnot)
 - Resolved some misunderstandings about Frama-C. ✓
- No work for proving correct the fix of the bug in v8 and v9.

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 - What changes are needed in the specifications?
 - How to automate them?
 - How to recognize cases that can't be automated (i.e., new algorithms)?
- Uptake from the Linux kernel community?

Conclusion

- Successfully proved properties of one Linux kernel function.
- Specifications and proofs somewhat resilient to code changes.
- Found a real bug that can have performance impact.
 - Keisuke's fix has been accepted into the Linux kernel.
- Lots more work to do.

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https://gitlab.inria.fr/lawall/swb_artifact